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| **Unit 1** | **Unit 2** | **Unit 3** | **Unit 4** | | **Unit 5** | **Unit 6** | **Unit 7** | **Unit 8** | **Unit9** | **Unit 10** | **Unit 11** | | **Unit 12** | **Unit 13** | **Unit 14** |
| **Multiples and Factors** | **Multiplying and Dividing Larger Numbers** | **Building Fractions for Addition and Subtraction** | **Applying Place Value** | | **Fraction Equivalence and Comparison** | **Measurement Conversions** | **Multiplicative Comparison** | **Solving Measurement Problems** | **Problem Solving With Fractions and Mixed Numbers** | **Angle Measurement** | **Multiplying Fractions by Whole Numbers** | | **Decimal Fractions and Notation** | **Attributes of 2-D Shapes** | **Problem Solving** |
| **10 days** | **15 days** | **8 days** | **12 days** | | **12 days** | **10 days** | **10 days** | **12 days** | **10 days** | **12 days** | **12 days** | | **10 days** | **12 days** | **15 days** |
| 4.OA.B.4 | 4.OA.A.3 | 4.NF.B.3a | 4.NBT.A.1 | | 4.NF.A.1 | 4.OA.A.1 | 4.OA.A.2 | 4.OA.A.3 | 4.NF.B.3c | 4.MD.C.5a | 4.OA.A.1 | | 4.NF.C.5 | 4.OA.C.5 | 4.OA.A.2 |
| 4.OA.C.5 | 4.NBT.B.5 | 4.NF.B.3b | 4.NBT.A.2 | | 4.NF.A.2 | 4.NBT.A.1 | 4.NBT.A.3 | 4.NBT.B.4 | 4.NF.B.3d | 4.MD.C.5b | 4.NF.B.4a | | 4.NF.C.6 | 4.MD.C.7 | 4.OA.A.3 |
| MP.3 | 4.NBT.B.6 | MP.4 | 4.NBT.A.3 | | MP.3 | 4.MD.A.1 | 4.MD.A.2 | 4.MD.A.2 | 4.MD.B.4 | 4.MD.C.6 | 4.NF.B.4b | | 4.NF.C.7 | 4.G.A.1 | 4.NBT.B.4 |
| MP.7 | 4.MD.A.3 |  | 4.NBT.B.4 | | MP.4 | MP.2 | MP.1 | MP.1 | MP.2 | 4.MD.C.7 | 4.NF.B.4c | | 4.MD.A.2 | 4.G.A.2 | 4.NBT.B.5 |
|  | MP.1 |  | MP.6 | |  | MP.6 |  | MP.2 | MP.4 | 4.G.A.1 | MP.1 | | MP.3 | 4.G.A.3 | 4.NBT.B.6 |
|  | MP.2 |  | MP.8 | |  | MP.7 |  | MP.6 |  | 4.G.A.2 | MP.6 | | MP.7 | MP.3 | MP.2 |
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| **Major Clusters** | | | | **Supporting Clusters** | | | | **Additional Clusters** | | | | **Other** | | | |
| OA – Operations and Algebraic Thinking  (1, 2, 3)  NBT – Number and Operations in Base Ten  (1, 2, 3, 4, 5, 6)  NF – Number and Operations – Fractions  (1, 2, 3, 4, 5, 6, 7) | | | | OA – Operations and Algebraic Thinking  (4)  MD – Measurement and Data  (1, 2, 3, 4) | | | | OA – Operations and Algebraic Thinking  (5)  MD – Measurement and Data  (5, 6, 7)  G – Geometry  (1, 2, 3) | | | | MP – Standards for Mathematical Practice | | | |

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| **Summary of Year for Grade 4 Mathematics** |
| In Grade 4, students should be given the opportunity for focused learning experiences in three critical areas:  (1) developing an understanding and fluency with multi-digit multiplication and of dividing to find quotients involving multi-digit dividends;  (2) developing an understanding of fraction equivalence, addition and subtraction of fractions with like denominators, and multiplication of fractions by whole numbers; and  (3) understanding that geometric figures can be analyzed and classified based on their properties, such as having parallel sides, perpendicular sides, particular angle measures, and symmetry.  Throughout Grade 4, students build on the work they completed in previous years by continuing to develop their understanding of numbers. They generalize their understanding of place value to 1,000,000. Students extend their understanding of the four operations to include multiplicative compare problems, operations with multi‐digit numbers, and multiplying fractions by whole numbers. Students develop their understanding of fractions to addition of fractions with like denominators and comparison and ordering of fractions with either like numerators or like denominators. The geometry focus is on angle measurement and line reasoning. |
| **Standards Clarification for Grade 4 Mathematics** |
| Some standards are included in multiple units to provide students with multiple opportunities to engage with the content. In the tables that follow, suggested focus areas and possible benchmarks for repeated standards are identified in the column labeled Standards Clarification. |
| **Mathematical Practices Recommendations for Grade 4** |
| Throughout Grade 4, students should continue to develop proficiency with the Common Core’s eight Standards for Mathematical Practice:  **1. Make sense of problems and persevere in solving them. 5. Use appropriate tools strategically.**  **2. Reason abstractly and quantitatively. 6. Attend to precision.**  **3. Construct viable arguments and critique the reasoning of others. 7. Look for and make use of structure.**  **4. Model with mathematics. 8. Look for and express regularity in repeated reasoning.**  These practices should become the natural way in which students come to understand and do mathematics. While, depending on the content to be understood or on the problem to be solved, any practice might be brought to bear, some practices may prove more useful than others. Opportunities for highlighting certain practices are indicated in different units in this document, but this highlighting should not be interpreted to mean that other practices should be neglected in those units. |
| **Fluency Requirements for Grade 4** |
| 4.NBT.B.4  Fluently add and subtract multi-digit whole numbers using the standard algorithm. |

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| **Unit 1: Multiples and Factors** | | **Possible time frame**:  10 days |
| In this unit students develop understanding of multiples and factors, applying their understanding of multiplication from the previous year. This understanding lays a strong foundation for generalizing strategies learned in previous grades to develop, discuss, and use efficient, accurate, and generalizable computational strategies involving multi-digit numbers. These concepts and the terms “prime” and “composite” are new to Grade 4, so they are introduced early in the year to give students ample time to develop and apply understanding. | | |
| **Supporting Cluster Standards** | | **Standards Clarification** |
| **Gain familiarity with factors and multiples.**  **4.OA.B.4** Find all factor pairs for a whole number in the range 1-100. Recognize that a whole number is a multiple of each of its factors. Determine whether a given whole number in the range 1-100 is prime or composite. | |  |
| **Additional Cluster Standards** | | **Standards Clarification** |
| **Generate and analyze patterns.**  **4.OA.C.5** Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself. *For example, given the rule, “Add 3” and the starting number 1, generate terms in the resulting sequence and observe that the terms appear to alternate between odd and even numbers. Explain informally why the numbers will continue to alternate in this way.* | | While working on **4.AO.C.5**, students use manipulatives to determine whether a number is prime or composite. Although there are shape patterns in arrays, the focus of this unit is number patterns. **4.OA.C.5** is repeated in Unit 13, where the focus will be on identifying shape patterns. |
| **Focus Standards for Mathematical Practice** | | |
| **MP.3** Construct viable arguments and critique the reasoning of others. | The focus of this unit is not necessarily to become fluent in finding all factor pairs, but to use student’s understanding of the concept and language to discuss the structure of multiples and factors. **(MP.3, MP.7)** | |
| **MP.7** Look for and make use of structure. |

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| **Unit 2: Multiplying and Dividing Larger Numbers** | | **Possible time frame**:  15 days |
| In this unit students continue using computational and problem-solving strategies, with a focus on building conceptual understanding of multiplication of larger numbers and division with remainders. Area and perimeter of rectangles provide one context for developing such understanding. | | |
| **Major Cluster Standards** | **Standards Clarification** | |
| **Use the four operations with whole numbers to solve problems.**  **4.OA.A.3** Solve multistep word problems posed with whole numbers and having whole answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.  **Use place value understanding and properties of operations to perform multi-digit arithmetic.**  **4.NBT.B.5** Multiply a whole number of up to four digits by a one-digit number, and multiply two two-digit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.  **4.NBT.B.6** Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models. | **4.OA.A.3** is the first time students are expected to interpret remainders based upon the context. The focus will be on multiplication and division. All four operations will be addressed in Unit 8, and the standard will be finalized in Unit 14.  NOTE: Grade 4 expectations in the NBT domain are limited to whole numbers less than or equal to 1,000,000. | |
| **Supporting Cluster Standards** | **Standards Clarification** | |
| **Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.**  **4.MD.A.3** Apply the area and perimeter formulas for rectangles in real world and mathematical problems. *For example, find the width of a rectangular room given the area of the flooring and the length, by viewing the area formula as a multiplication equation with an unknown factor.* | **4.MD.A.3** provides context of area and perimeter of rectangles for problem solving. Introduced to formulas in this unit and make sense of them using prior work with area and perimeter. | |

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| **Focus Standards for Mathematical Practice** | |
| **MP.1** Make sense of problems and persevere in solving them. | Students make sense of multi-step problems **(MP.1)** and reason about how the formulas connect to the context **(MP.2)**. The use of generalized strategies and formulas provides an opportunity to investigate and use regularity in repeated reasoning **(MP.8).** |
| **MP.2** Reason abstractly and quantitatively. |
| **MP.8** Look for and express regularity in repeated reasoning. |

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| **Unit 3: Building Fractions for Addition and Subtraction** | | **Possible time frame**:  8 days |
| In this unit students extend their prior knowledge of unit fractions with denominators of 2, 3, 4, 6, and 8 from Grade 3 to include denominators of 5, 10, 12, and 100. In Grade 4, they use their understanding of partitioning to find unit fractions to compose and decompose fractions in order to add fractions with like denominators. This is the foundational for further work with fractions later in the year, such as comparing fractions and multiplying fractions by a whole number. | | |
| **Major Cluster Standards** | | **Standards Clarification** |
| **Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers.**  **4.NF.B.3** Understand a fraction a/b with a > 1 as a sum of fraction 1/b.   1. Understand addition and subtraction of fractions as joining and separation parts referring to the same whole. 2. Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. *Examples: 3/8 = 1/8 + 1/8 + 1/8; 3/8 = 1/8 + 2/8; 2 1/8 = 1 + 1 + 1/8 = 8.8 + 8/8 + 1/8.* | | NOTE: Grade 4 expectations in the NF domain are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100. |
| **Focus Standards for Mathematical Practice** | | |
| **MP.4** Model with mathematics. | Students use visual and concrete models to represent a fractional situation in order to add and subtract fractions. (**MP.4**). | |

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| **Unit 4: Applying Place Value** | | **Possible time frame**:  12 days |
| The focus of this unit is to provide students time to develop and practice efficient addition and subtraction of multi-digit whole numbers while developing place value concepts. | | |
| **Major Cluster Standards** | | **Standards Clarification** |
| **Generalize place value understanding for multi-digit whole numbers.**  **4.NBT.A.1** Recognize that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. *For example, recognize that 700 ÷ 70 = 10 by applying concepts of place value and division*.  **4.NBT.A.2** Read and write multi-digit whole numbers using base-ten numerals, number names, and expanded form. Compare two multi-digit numbers based on meanings of the digits in each place, using >, =, and < symbols to record the results of comparisons.  **4.nbt.a.3** Use place value understanding to round multi-digit whole numbers to any place.  **Use place value understanding and properties of operations to perform multi-digit arithmetic.**  **4.NBT.B.4** Fluently add and subtract multi-digit whole numbers using the standard algorithm. | | **4.NBT.A.1** will be revisited in Unit 6 connected to conversions within the metric system of measurement.  **4.NBT.A.3** will be revisited in Unit 7 with multiplication and division as a context.  **4.NBT.B.4** will be revisited in Unit 8 and finalized in Unit 14 for fluency in addition and subtraction of multi-digit whole numbers.  NOTE: Grade 4 expectations in the NBT domain are limited to whole numbers less than or equal to 1,000,000. |
| **Focus Standards for Mathematical Practice** | | |
| **MP.6** Attend to precision. | Students use the structure of the base-ten system to generalize their strategies and to discuss reasonableness of their computations and work towards fluency. (**MP.6, MP.8**). | |
| **MP.8** Look for and express regularity in repeated reasoning. |

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| **Unit 5: Fraction Equivalence and Comparison** | | **Possible time frame**:  12 days |
| In this unit students develop an understanding of fraction equivalence and various methods for comparing fractions. Students should understand that when comparing fractions, it is not always necessary to generate equivalent fractions. Other methods, such as comparing fractions to a benchmark, can be used to discuss relative sizes. The justification of comparing or generating equivalent fractions using visual models is an emphasis of this unit.¹ | | |
| **Major Cluster Standards** | | **Standards Clarification** |
| **Extend understanding of fraction equivalence and ordering.**  **4.NF.A.1** Explain why a fraction a/b is equivalent to a fraction (n x a)/(n x b) by using visual fraction models, with attention to how the number and size of the parts differ even though the two fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.  **4.NF.A.2** Compare two fractions with different numerators and different denominators, e.g., by creating common denominators or numerators, or by comparing to a benchmark fraction such as 1/2 . Recognize that comparisons with symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction model. | | NOTE: Grade 4 expectations in the NF domain are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100. |
| **Focus Standards for Mathematical Practice** | | |
| **MP.3** Construct viable arguments and critique the reasoning of others. | Students justify their methods for generating equivalent fractions and comparing fractions by using their conceptual understanding and models (**MP.3, MP.5**). | |
| **MP.4** Model with mathematics. |

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| **Unit 6: Measurement Conversions** | | **Possible time frame**:  10 days |
| In this unit students build a conceptual understanding of the relative sizes of units of measure within a single system of measurement. Measurement conversions are used to introduce multiplication as a comparison. The concepts in this unit are foundational for the concepts in unit 7 and unit 8. | | |
| **Major Cluster Standards** | **Standards Clarification** | |
| **Use the four operations with whole numbers to solve problems.**  **4.OA.A.1** Interpret a multiplication equation as a comparison, e.g., interpret 35 = 5 x 7 as a statement that 35 is 5 times as many as 7 and 7 times as many as 5. Represent verbal statements of multiplicative comparisons as multiplication equations.  **Generate place value understanding for multi-digit whole numbers.**  **4.NBT.A.1** Recognize that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. *For example, recognize that 700 ÷ 70 = 10 by applying concepts of place value and division.* | **4.OA.A.1** is repeated in unit 11, in which the focus is on multiplication of fractions.  **4.NBT.A.1** was addressed in unit 4, in which the focus was on addition and subtraction. In this unit, metric measurement provides an opportunity to deepen the students’ understanding of place value in relation to multiples of 10.  NOTE: Grade 4 expectations in the NBT domain are limited to whole numbers less than or equal to 1,000,000. | |
| **Supporting Cluster Standards** | **Standards Clarification** | |
| **Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.**  **4.MD.A.1** Know relative sizes of measurement units within one system of units including km, m, cm; kg, g; lb, oz.; l, ml; hr, min, sec. Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. Record measurement equivalents in two-column table. *For example, know that 1 ft is 12 times as long as 1 in. Express the length of a 4 ft snake as 48 in. Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3, 36), …* | **4.MD.A.1** Introduces units of measure new to Grade 4. | |

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| **Focus Standards for Mathematical Practice** | |
| **MP.2** Reason abstractly and quantitatively. | In this unit students look for patterns in different measurement systems (**MP.2**, **MP.7**) and discuss precisely how many times larger one unit is than another (**MP.6**) |
| **MP.6** Attend to precision. |
| **MP.7** Look for and make use of structure. |

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| **Unit 7: Multiplicative Comparison** | | **Possible time frame**:  10 days |
| In this unit students are introduced to multiplicative compare problems, extending their conceptual work with multiplicative comparison from unit 6. For students to develop this concept, they must be provided rich problem situations that encourage them to make sense of the relationships among the quantities involved, model the situation, and check their solution using a different method. CCSSM Table 2 is an important resource for understanding multiplicative comparison problems, which are new to Grade 4 students.[[1]](#footnote-1) | | |
| **Major Cluster Standards** | | **Standards Clarification** |
| **Use the four operations with whole numbers to solve problems.**  **4.OA.A.2** Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison.  **Generalize place value understanding for multi-digit whole numbers.**  **4.NBT.A.3** Use place value understanding to round multi-digit whole numbers to any place. | | **4.OA.A.2** is also addressed in unit 14 because of the time it takes to master the concepts and its importance to future mathematics.  **4.OA.A.2** For information on comparison problems, see the Glossary, Table 2 in CCSSM page 89.  **4.NBT.A.3** was addressed in unit 4 with a focus on addition and subtraction. In this unit, the focus is on multiplication and division.  NOTE: Grade 4 expectations in the NBT domain are limited to whole numbers less than or equal to 1,000,000. |
| **Supporting Cluster Standards** | | **Standards Clarification** |
| **Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.**  **4.MD.A.2 Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.** | | **4.MD.A.2 is used as a context for multiplicative compare problems with whole numbers only. This standard is revisited in unit 8 to include the four operations, and addressed in unit 12 with decimal fractions.** |
| **Focus Standards for Mathematical Practice** | | |
| **MP.1** Make sense of problems and persevere in solving them. | Students use charts and diagrams to explain their own methods as well as make sense of approaches taken by others (**MP.1**) | |

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| **Unit 8: Solving Measurement Problems** | **Possible time frame**:  12 days |
| In this unit students combine competencies from different domains to solve measurement problems using the four operations. Measurement is included in this unit to provide a context for problem solving. All of the problem types in Table 1 and Table 2 on pages 88 and 89 of the Common Core State Standards for Mathematics should be addressed in this unit. | |
| **Major Cluster Standards** | **Standards Clarification** |
| **Use the four operations with whole numbers to solve problems.**  **4.OA.A.3** Solve multistep word problems posed with whole number and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.  **Use place value understanding properties of operations to perform multi-digit arithmetic.**  **4.NBT.B.4** Fluently add and subtract multi-digit whole numbers using the standard algorithm. | **4.OA.A.3** and **4.NBT.B.4** are repeated here to include all four operations and will be finalized in unit 14. Repeating these standards throughout the year provides students multiple opportunities to develop these skills.  NOTE: Grade 4 expectations in the NBT domain are limited to whole numbers less than or equal to 1,000,000. |
| **Supporting Cluster Standards** | **Standards Clarification** |
| **Measurement and Data – 4.MD**  **Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.**  **4.MD.A.2** Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale. | **4.MD.A.2** is repeated from the previous unit, but in this unit the emphasis is on using the four operations and all problem types. This standard will be finalized in unit 12 to include decimal fractions. |

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| **Focus Standards for Mathematical Practice** | |
| **MP.1** Make sense of problems and persevere in solving them. | Students use various diagrams and precise language to solve measurement problems and explain their strategies. (**MP.1, MP.6**). The make connections between abstract representations and the problem situations (**MP.2**). |
| **MP.2** Reason abstractly and quantitatively. |
| **MP.6** Attend to precision. |

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| **Unit 9: Problem Solving with Fractions and Mixed Numbers** | | **Possible time frame**:  10 days |
| In this unit students will use their understanding of adding and subtracting fractions and generating equivalent fractions to solve problems involving fractions and mixed numbers. Students rely on their previous work with whole number as fractions to compose and decompose whole numbers into fractional quantities. Data is used in this unit to support students’ understanding of fractional quantities both smaller and larger than 1. | | |
| **Major Cluster Standards** | | **Standards Clarification** |
| **Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers.**  **4.NF.B.3** Understand a fraction a/b with a > 1 as a sum of fractions 1/b.   1. Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with an equivalent fraction, and /or by using properties of operations and the relationship between addition and subtraction. 2. Solve word problems involving addition and subtraction of fractions referring to same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem. | | NOTE: Grade 4 expectations in the NF domain are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100. |
| **Supporting Cluster Standards** | | **Standards Clarification** |
| **Measurement and Data – 4.MD**  B. Represent and interpret data.  Make a line plot to display a data set of measurements in fractions a unit (1/2, 1/4, 1/8). Solve problems involving addition and subtraction of fractions by using information presented in line plots. For example, from a line plot find and interpret the difference in length between the longest and shortest specimens in an insect collection. | | **4.MD.B.4** extends students’ work from Grade 3 with simple fractions on a line plot (**3.MD.B.4**) to include eighths and to now solve addition and subtraction problems using the data. |
| **Focus Standards for Mathematical Practice** | | |
| **MP.2** Reason abstractly and quantitatively. | Students reason about fractions by using abstract models to represent both the data and the fractional quantities (**MP.2, MP.4**) | |
| **MP.4** Model with mathematics. |

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| **Unit 10: Angle Measurement** | | **Possible time frame**:  12 days |
| This unit is an introduction to angles and angle measurement. Students start this unit drawing points, lines, segments, rays and angles since it is foundational to the other standards in this unit. Students use their understanding of equal partitioning and unit measurement to understand angle and turn measure. | | |
| **Additional Cluster Standards** | | **Standards Clarification** |
| **Geometric measurement: understand concepts of angle and measure angles.**  **4.MD.C.5** Recognize angles as geometric shapes that are formed wherever two rays share a common endpoint, and understand concepts of angle measurement.   1. An angle is measured with reference to a circle with its center at the common endpoint of the rays, by considering the fraction of the circular arc between the point where the two rays intersect the circle. An angle that turns through 1/360 of a circle is called a “one-degree angle,” and can be used to measure angles. 2. An angle that turns through *n* one-degree angles is said to have an angle measure of *n* degrees.   **4.MD.C.6** Measure angles in whole-number degrees using a protractor. Sketch angles of specified measure.  **4.MD.C.7** Recognize angle measure as additive. When an angle is decomposed into non-overlapping parts, the angle measure of the whole is the sum of the angle measures of the parts. Solve addition and subtraction problems to find unknown angles on a diagram in real world and mathematical problems, e.g., by using an equation with a symbol for the unknown angle measure.  **Draw and identify lines and angles, and classify shapes by properties of their lines and angles.**  **4.G.A.1** Draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines, identify these in two dimensional figures.  **4.G.A.2** Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a specified size. Recognize right triangles as a category, and identify right triangles. | | In this unit, **4.G.A.1** focuses on drawing points, lines, line segments, rays, and different types of angles. The standard will be addressed in its entirety in unit 13.  **4.G.A.2** focuses on classifying two-dimensional figures based on the measurement of the angles. The standard will be addressed in its entirety in unit 13. |
| **Focus Standards for Mathematical Practice** | | |
| **MP.4** Model with mathematics. | Students select and use a protractor to measure angles and represent the angles with drawings (**MP.4, MP.5**) | |
| **MP.5** Use appropriate tools strategically. |

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| **Unit 11: Multiplying Fractions by Whole Numbers** | | **Possible time frame**:  12 days |
| In this unit students apply their understanding of composing and decomposing fractions to develop a conceptual understanding of multiplication of a fraction by a whole number. Students also use and extend their previous understandings of operations with whole numbers and relate that understanding to fractions. | | |
| **Major Cluster Standards** | | **Standards Clarification** |
| **Use the four operations with whole numbers to solve problems.**  **4.OA.A.1** Interpret a multiplication equation as a comparison, e.g., interpret 35 = 5 x 7 as a statement that 35 is 5 times as many as 7 and 7 times as many as 5. Represent verbal statements of multiplicative comparisons as multiplication equations.  **Build fractions from unit fractions by applying and extending previous understanding of operations on whole numbers.**  **4.NF.B.4** Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.   1. Understand a fraction a/b as a multiple of 1/b. *For example, use a visual fraction model to represent 5/4 as the product 5 x (1/4), recording the conclusion by the equation 5/4 = 5 x (1/4)*. 2. Understand a multiple of a/b as a multiple of 1/b, and use this understanding to multiply a fraction by a whole number. *For example, use a visual fraction model to express 3 x (2/5) as 6 x (1/5), recognizing this product as 6/5. (In general, n x (a/b) = (n x a)/b.)* 3. Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual models and equations to represent the problem. *For example, if each person at a party will eat 3/8 of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie?* | | **4.OA.A.1** is readdressed in this unit to include multiplication of fractions and apply the understanding of “times as much” (i.e. multiplication as comparison) to multiplying a fraction by a whole number.  NOTE: Grade 4 expectations in the NF domain are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100. |
| **Focus Standards for Mathematical Practice** | | |
| **MP.1** Make sense of problems and persevere in solving them. | Students use precise language to communicate their comprehension of the problem situations and defend their various solution methods. (**MP.1, MP.6**) | |
| **MP.6** Attend to precision. |

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| **Unit 12: Decimal Fractions and Notation** | | **Possible time frame**:  10 days |
| In this unit of study students use their previous work with fractions to represent special fractions in a new way. Students use their understanding of equivalent fractions to begin to use decimal notation – however, it is not the intent at this grade level to connect this notation to the base-ten system. The focus is on solving work problems involving simple fractions or decimals.⁹ Work with money can support this work decimal fractions. | | |
| **Major Cluster Standards** | | **Standards Clarification** |
| **Understand decimal notation for fractions, and compare decimal fractions.**  **4.NF.C.5** Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100. *For example, express 3/10 as 30/100 and add 3/10 + 4/100 = 34/100.*  **4.NF.C.6**Use decimal notation for fractions with denominators 10 or 100. *For example, rewrite 0.62 as 62/100; describe a length as 0.62 meters; locate 0.62 on a number line diagram.*  **4.NF.C.7** Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols >, =, <, and justify the conclusions, e.g., by using a visual model. | | **4.NF.C.5** Students who can generate equivalent fractions can develop strategies for adding fractions with unlike denominators in general. But addition and subtraction with unlike denominators in general is not a requirement at this grade.  NOTE: Grade 4 expectations in the NF domain are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100. |
| **Supporting Cluster Standards** | | **Standards Clarification** |
| **Solve problems involving measurement and conversion from a larger unit to a smaller unit.**  **4.MD.A.2** Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale. | | **4.MD.A.2** was addressed in unit 7. It is important to note that students are not expected to do computations with quantities in decimal notation. Students can use visual fraction models to solve problems involving simple fractions or decimals. |
| **Focus Standards for Mathematical Practice** | | |
| **MP.3** Construct viable arguments and critique the reasoning of others. | Students compare decimals fractions and justify their comparisons using either a fraction model or their understanding of the notation (**MP.3, MP.7**). | |
| **MP.7** Look for and make use of structure. |

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| **Unit 13: Attributes of 2-D Shapes** | **Possible time frame**:  12 days |
| In this unit students develop their spatial reasoning skills by using a wide variety of attributes to talk about 2-dimenstional shapes. Students analyze geometric figures based on angle measurement, parallel and perpendicular lines, and symmetry. | |
| **Additional Cluster Standards** | **Standards Clarification** |
| **Generate and analyze patterns.**  **4.OA.C.5** Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself. *For example, given the rule, “Add 3” and the starting number 1, generate terms in the resulting sequence and observe that the terms appear to alternate between odd and even numbers. Explain informally why the numbers will continue to alternate in this way.*  **Geometric measurement: understand concepts of angle and measure angles.**  **4.MD.C.7** Recognize angle measure as additive. When an angle is decomposed into non-overlapping parts, the angle measure of the whole is the sum of the angle measures of the parts. Solve addition and subtraction problems to find unknown angles on a diagram in real world and mathematical problems, e.g., by using an equation with a symbol for the unknown angle measure.  **Draw and identify lines and angles, and classify shapes by properties of their lines and angles.**  **4.G.A.1** Draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines. Identify these in two-dimensional figures.  **4.G.A.2** Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a specified size. Recognize right triangles as a category, and identify right triangles.  **4.G.A.3** Recognize a line of symmetry for a two-dimensional figure as a line across the figure such that the figure can be folded along the line into matching parts. Identify line-symmetric figures and draw lines of symmetry. | In this unit, **4.OA.C.5** includes repeated and growing shape patterns.¹⁰  **4.G.A.1** and **4.G.A.2** were first addressed in unit 10, and are addressed in their entirety in this unit to include perpendicular and parallel lines. |

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| **Focus Standards for Mathematical Practice** | |
| **MP.3** Construct viable arguments and critique the reasoning of others. | The concepts in this unit lend themselves to using technology applications (**MP.5**).  Students understand that geometric figures can be classified by analyzing various properties (**MP.7**) and justify their conclusions by using viable arguments (**MP.3**). |
| **MP.5** Use appropriate tools strategically. |
| **MP.7** Look for and make use of structure. |

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| **Unit 14: Problem Solving** | | **Possible time frame**:  15 days |
| This is a culmination unit in which students focus on problem solving in order to demonstrate fluency with the standard algorithms in addition and subtraction. All standards in this unit have been addressed in prior units. These concepts require greater emphasis due to the depth of the ideas, the time they take to master, and/or their importance to future mathematics. | | |
| **Major Cluster Standards** | | **Standards Clarification** |
| **Use the four operations with whole numbers to solve problems.**  **4.OA.A.2** Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using drawing and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison.  **4.OA.A.3** Solve multistep word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.  **Use place value understanding and properties of operations to perform multi-digit arithmetic.**  **4.NBT.B.4** Fluently add and subtract multi-digit whole numbers using the standard algorithm.  **4.NBT.B.5** Multiply a whole number of up to four digits by a one-digit whole number, and multiply two two-digit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.  **4.NBT.B.6** Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models. | | NOTE: Grade 4 expectations in the NBT domain are limited to whole numbers less than or equal to 1,000,000. |
| **Focus Standards for Mathematical Practice** | | |
| **MP.2** Reason abstractly and quantitatively. | In demonstrating fluency, students explain and flexibly use properties of operations and place value to solve problems, looking for shortcuts and applying generalized strategies (**MP.2, MP.8**). | |
| **MP.8** Look for and express regularity in repeated reasoning. |

1. For additional information on multiplication “compare” problems, Table 2 on page 89 in the Common Core State Standards for Mathematics. [↑](#footnote-ref-1)